



# Motivation

Features of the current crisis:

- Increased default in the U.S. mortgage market
- Contagion to securitized products and credit markets
- Interbank markets fail to act as a conduit for monetary policy
- Collapse of systemically important financial institutions

DSGE models are inappropriate for financial stability analysis.

- Representative agent models: no trade, no default
- Money is a veil
- No financial frictions: default risk, banks, contagion
- Limited scope for welfare improving economic policy: markets are complete



# Our Model

## Monetary General Equilibrium Model with Commercial Banks, Collateral, Securitisation and Default (**MEBCSD**)

- Non-trivial quantity theory of money
- Term structure of interest rates depends on aggregate liquidity and default risk
- Fisher effect
- Financial fragility is an equilibrium outcome
- Constrained inefficient equilibrium allocations
- Assessment of various policies for crisis management and prevention

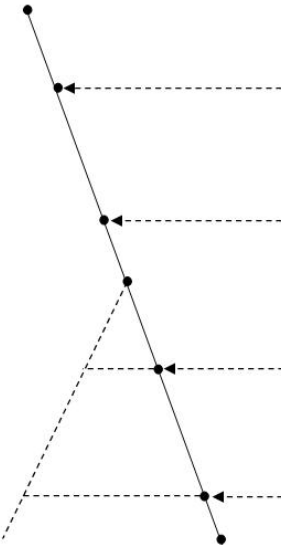


# Results

- Interest rate instrument is preferable to the monetary base instrument in times of financial distress
- CPI should include an appropriate measure of housing prices
- Central Banks' Financial Stability objective is primarily achieved by regulating systemic financial agents



# Time Structure



- t=0
1. OMO's and government bond sales (CB and cb)
  2. Short term credit markets (cb and H)
  3. Mortgage markets meet (cb and H)
  4. Mortgage Backed Asset markets meet (cb and IB)
  5. Interbank market meets (cb)
  6. Wholesale Money market meets (cb and IB, HF)
  7. Deposit market meets (cb and H)
- t=1
1. Trade between households (H)
  2. Trade in CDO's market (cb and IB, HF)
  3. Short term loans settlement (CB, cb, H)
  4. Consumption (H)
- Nature chooses a state
1. OMO's and government bond sales (CB and cb)
  2. Short term credit markets (cb and H)
  3. Mortgage market settles (H and cb)
  4. CDO markets settles (IB and HF)
  5. Wholesale Money market settles (cb and IB, HF)
  6. Interbank market settles (cb)
  7. Deposit market settles (cb and H)
1. Trade between households (H)
  2. Short term loans settlement (CB, cb, H)
  3. Consumption (H, IB, HF)
  4. Liquidation of Commercial banks (cb and CB)





# Money and Collateral

## Money

- Introduced by a cash-in-advance (liquidity) transaction technology
- Enters the system as *outside* or *inside* money

## Collateral

- Household  $\alpha$  pledges purchased housing as collateral when he takes out the mortgage
- If  $\alpha$  defaults on the mortgage, the bank seizes the collateral and offers it for sale in the next period (US's 'walk away' option)

# Default

Two types of Default:

- **Discontinuous** mortgage default. Household  $\alpha$  defaults on his mortgage if

$$(p_{22} b_{02}^{\alpha} / p_{02}) \leq (\bar{\mu}^{\alpha})$$

(collateral's worth)  $\leq$  (mortgage debt)

- **Continuous** default in the interbank and wholesale money markets: agents choose a repayment rate satisfying the *On the Verge Condition* (for  $k = \{\delta, \psi, \phi\}$ ):

$$\left( \frac{\partial \Pi^k}{\partial \bar{v}_s^k} \right) = \bar{\tau}_s^k$$

(marginal utility of default) = (bankruptcy penalty)

# Securitisation

Scarcity of collateral incentivizes agents to stretch it by using it many times.

- The investment bank ( $\psi$ ) buys the mortgage from bank  $\gamma$  at a price  $p^\alpha$  in the MBS's market
- The investment bank ( $\psi$ ) structures a CDO by attaching a Credit Default Swap (CDS) to the MBS
- The hedge fund ( $\phi$ ) purchases the CDO at a price  $\tilde{q}^\alpha$
- CDO's gross returns:

$$R^{CDO} = \left[ \frac{(1 + \bar{r}^{\gamma\alpha}) / \tilde{q}^\alpha}{1} \right]$$

- The investment bank bears the mortgage and CDS risk

# Household $\alpha$ 's Optimisation Problem

$$\begin{aligned}
 \max_{q_{s^*1}^\alpha, b_{s^*2}^\alpha, \mu_{s^*}^\alpha, \bar{\mu}^\alpha} U^\alpha &= u(e_{01}^\alpha - q_{01}^\alpha) + u\left(\frac{b_{02}^\alpha}{p_{02}}\right) + \sum_{s \in S} \omega_s u(e_{s1}^\alpha - q_{s1}^\alpha) \\
 &+ \sum_{s \in S_1^\alpha} \omega_s u\left(\frac{b_{02}^\alpha}{p_{02}} + \frac{b_{s2}^\alpha}{p_{s2}}\right) + \sum_{s \notin S_1^\alpha} \omega_s u\left(\frac{b_{s2}^\alpha}{p_{s2}}\right)
 \end{aligned}$$

s. t.

$$b_{02}^\alpha \leq \frac{\bar{\mu}^\alpha}{(1 + \bar{r}^\alpha)} + \frac{\mu_0^\alpha}{(1 + r_0^\alpha)} + e_{m,0}^\alpha$$

i.e. housing expenditure at  $t=0 \leq$  mortgage loan + short-term borrowing + private monetary endowments at  $t=0$

$$\mu_0^\alpha \leq p_{01} q_{01}^\alpha$$

i.e. short term loan repayment at  $t=0 \leq$  goods sales revenues at  $t=0$

# Household $\alpha$ 's Optimisation Problem

$$b_{s2}^{\alpha} + \bar{\mu}^{\alpha} \leq \frac{\mu_s^{\alpha}}{(1 + r_s^{\gamma})} + e_{m,s}^{\alpha} \quad \text{for } s \in S_1^{\alpha}$$

i.e. housing expenditure at  $s \in S_1^{\alpha}$  + mortgage repayment  $\leq$  short-term borrowing + private monetary endowments at  $s \in S_1^{\alpha}$

$$b_{s2}^{\alpha} \leq \frac{\mu_s^{\alpha}}{(1 + r_s^{\gamma})} + e_{m,s}^{\alpha} \quad \text{for } s \notin S_1^{\alpha}$$

i.e. housing expenditure at  $s \notin S_1^{\alpha}$   $\leq$  short-term borrowing + private monetary endowments at  $s \notin S_1^{\alpha}$

$$\mu_s^{\alpha} \leq p_{s1} q_{s1}^{\alpha}$$

i.e. short term loan repayment  $\leq$  goods sales revenues at  $t=0$

$$q_{s^*1}^{\alpha} \leq e_{s^*1}^{\alpha}$$

i.e. quantity of goods sold at  $s \in S^*$   $\leq$  goods endowments at  $s \in S^*$

# Household $\theta$ 's Optimisation Problem

$$\max_{q_{s^*2}^\theta, b_{s^*1}^\theta, \mu_{s^*}^\theta, \bar{d}^\theta} U^\theta = u\left(\frac{b_{01}^\theta}{p_{01}}\right) + u\left(e_{02}^\theta - q_{02}^\theta\right) + \sum_{s \in S} \omega_s u\left(\frac{b_{02}^\theta}{p_{02}}\right) + \sum_{s \in S} \omega_s u\left(e_{02}^\theta - q_{s0}^\theta - q_{s2}^\theta\right)$$

s. t.

$$b_{01}^\theta + \bar{d}^\theta \leq \frac{\mu_0^\theta}{1 + r_0^\delta} + e_{m,0}^\theta$$

i.e. goods expenditure at  $t=0$  + inter-period deposits  $\leq$  short-term borrowing + private monetary endowments at  $t=0$

$$\mu_0^\theta \leq p_{02} q_{02}^\theta$$

(i.e. short term loan repayment at  $t=0 \leq$  housing sales revenues at  $t=0$ )

# Household $\theta$ 's Optimisation Problem

$$b_{s1}^{\theta} \leq \frac{\mu_s^{\theta}}{1 + r_s^{\delta}} + \bar{d}^{\theta} (1 + \bar{r}_d^{\gamma}) + e_{m,s}^{\theta} \quad \text{for } s \in S$$

i.e. goods expenditure at  $s \in S \leq$  short-term borrowing + deposits and interest payment + private monetary endowments at  $s \in S$

$$\mu_s^{\theta} \leq p_{s2} q_{s2}^{\theta}$$

i.e. short term loan repayment at  $s \in S \leq$  housing sales revenues at  $s \in S$

$$q_{s*2}^{\theta} \leq e_{s2}^{\theta} - q_{02}^{\theta}$$

i.e. number of housing units sold at  $s \in S \leq$  endowment of housing at  $t=0$  - units of housing sold at  $s \in S$



# Bank $\gamma$ 's Optimisation Problem

$$\max_{m_{s^*2}^\gamma, \bar{m}^\alpha, d_{s^*}^{G\gamma}, \bar{d}^\gamma, \pi_s^\gamma} \Pi^\gamma = \sum_{s \in S} \omega_s \left( \pi_s^\gamma - c^\gamma (\pi_s^\gamma)^2 \right)$$

s.t.

$$d_0^{G\gamma} + m_0^\gamma + \bar{m}^\alpha + \bar{d}^\gamma \leq e_0^\gamma + (\bar{\mu}_d^\gamma / 1 + \bar{r}_d^\gamma)$$

i.e. deposits in the repo market + short-term lending + mortgage extension + interbank lending  $\leq$  capital endowment at  $t=0$  + consumer deposits

$$d_s^{G\gamma} + m_s^\gamma + \bar{\mu}_d^\gamma \leq e_s^\gamma + \pi_0^\gamma + \bar{R}_s^\delta \bar{d}^\gamma (1 + \bar{\rho})$$

i.e. short-term lending + deposits in the repo market at  $s \in S$  + deposits repayment  $\leq$  capital endowment at  $s \in S$  + accumulated profits + interbank loan repayments at  $s \in S$

$$\pi_0^\gamma = m_0^\gamma (1 + r_0^\gamma) + d_0^{G\gamma} (1 + \rho_0^{CB}) + p^\alpha \bar{m}^\alpha$$

i.e. profits at ( $t=0$ ) = short term loan repayment + repo deposits and interest payment at  $t=0$  + MBS's sales revenues

$$\pi_s^\gamma = m_s^\gamma (1 + r_s^\gamma) + d_s^{G\gamma} (1 + \rho_s^{CB})$$

i.e. profits at  $s \in S$  = short term loan repayment + repo deposits and interest payment at  $s \in S$

# Bank $\delta$ 's Optimisation Problem

$$\max_{m_{s^*2}^\delta, \bar{m}, \mu_{s^*}^{G\delta}, \bar{\mu}^\delta, \mu_{s^*}^\delta, \bar{v}_s^\delta, \pi_s^\gamma} \Pi^\delta = \sum_{s \in S} \omega_s \left( \pi_s^\delta - c^\delta (\pi_s^\delta)^2 \right) - \sum_{s \in S} \omega_s \bar{r}_s^\delta [\bar{D}_s^\delta]^+$$

s.t.

$$m_0^\delta + \bar{m} \leq e_0^\delta + \frac{\mu_0^{G\delta}}{1 + \rho_0^{CB}} + \frac{\bar{\mu}^\delta}{1 + \bar{\rho}}$$

i.e. short-term lending at t=0 + wholesale money market credit extension  $\leq$  capital endowment + short-term borrowing in the repo market at t=0 + interbank borrowing

$$\mu_0^{G\delta} \leq m_0^\delta (1 + r_0^\delta)$$

i.e. repo loan repayment at t=0  $\leq$  short-term loan repayment at t=0

$$m_s^\delta + \bar{v}_s^\delta \bar{\mu}^\delta \leq e_s^\delta + \frac{\mu_s^{G\delta}}{1 + \rho_s^{CB}} + \bar{R}_s \bar{m} (1 + \bar{r})$$

i.e. short-term lending + interbank loan repayment at  $s \in S \leq$  capital endowment + wholesale money market loan repayment short-term loan repayment at  $s \in S$

$$\pi_s^\delta = m_s^\delta (1 + r_s^\delta) - \mu_s^{G\delta}$$

i.e. profits at  $s \in S =$  short term loan repayment - repo loan repayment at  $s \in S$

# Investment Bank ( $\psi$ )'s Optimisation Problem

$$\max_{\tilde{m}^\alpha, \bar{\mu}^\psi, \bar{v}_s^\psi} \Pi^\psi = \sum_{s \in S} \omega_s \pi_s^\psi - \sum_{s \in S} \omega_s \bar{r}_s^\psi \left[ \bar{D}_s^\psi \right]^+$$

s. t.

$$\tilde{m}^\alpha \leq e_0^\psi + \frac{\bar{\mu}^\psi}{1 + \bar{r}}$$

i.e. expenditure in MBS's  $\leq$  capital endowments at  $t=0$  + wholesale money market borrowing

$$\bar{v}_s^\psi \bar{\mu}^\psi \leq \frac{\tilde{m}^\alpha}{p^\alpha} \tilde{q}^\alpha \quad \text{for } s \in S_1^\alpha$$

i.e. whole sale money market loan repayment at  $s \in S_1^\alpha \leq$  CDO's sales revenues + capital endowments at  $s \in S_1^\alpha$

$$\tilde{m}^\alpha \tilde{q}^\alpha + \bar{v}_s^\psi \bar{\mu}^\psi \leq e_s^\psi + \left( \tilde{q}^\alpha + \frac{b_{02}^\alpha p_{22}}{\tilde{m}^\alpha p_{02}} \right) \frac{\tilde{m}^\alpha}{p^\alpha} \quad \text{for } s \notin S_1^\alpha$$

i.e. CDS settlement payment + wholesale money market loan repayment at  $s \notin S_1^\alpha \leq$  capital endowment at  $s \notin S_1^\alpha$  + CDO's sales revenues + collateral sales revenues

# Hedge Fund ( $\phi$ )'s Optimisation Problem

$$\max_{\bar{\mu}^\phi, \hat{m}^\alpha, \bar{v}_{s^*}^\phi} \Pi^\phi = \sum_{s \in S} \omega_s \pi_s^\phi - \sum_{s \in S} \omega_s \bar{r}_s^\phi \left[ \bar{D}_s^\phi \right]^+$$

s.t.

$$\hat{m}^\alpha \leq \frac{\bar{\mu}^\phi}{1 + \bar{r}}$$

i.e. expenditure in the CDO's market  $\leq$  wholesale money market borrowing

$$\bar{v}_s^\phi \bar{\mu}^\psi \leq \frac{\hat{m}^\alpha}{\bar{q}^\alpha} (1 + \bar{r}^{\gamma^\alpha}) \quad \text{for } s \in S_1^\alpha$$

i.e. wholesale money market loan repayment  $\leq$  CDO's payoffs at  $s \in S_1^\alpha$

$$\bar{v}_s^\phi \bar{\mu}^\psi \leq \hat{m}^\alpha \quad \text{for } s \notin S_1^\alpha$$

i.e. wholesale money market loan repayment  $\leq$  CDO's payoffs at  $s \notin S_1^\alpha$

# Market Clearing Conditions

## Goods Market

$$p_{01} = \frac{b_{01}^{\theta}}{q_{01}^{\alpha}}$$
$$p_{s1} = \frac{b_{s1}^{\theta}}{q_{s1}^{\alpha}} \quad \text{for } s \in S$$

## Housing Market

$$p_{02} = \frac{b_{02}^{\alpha}}{q_{02}^{\theta}}$$
$$p_{s2} = \frac{b_{s2}^{\alpha}}{q_{s2}^{\theta}} \quad \text{for } s \in S_1^{\alpha}$$
$$p_{s2} = \frac{b_{s2}^{\alpha}}{q_{s2}^{\theta} + b_{02}^{\alpha}/p_{02}} \quad \text{for } s \notin S_1^{\alpha}$$

# Market Clearing Conditions

## Mortgage Market

$$(1 + \bar{r}^{\gamma\alpha}) = \frac{\bar{\mu}^{\alpha}}{\bar{m}^{\alpha}}$$

Clearing conditions for effective returns on mortgages

$$(1 + \bar{r}_s^{\gamma\alpha}) = \begin{cases} (1 + \bar{r}^{\gamma\alpha}) & \text{for } s \in S_1^{\alpha} \\ \left( \frac{p_{22} b_{02}^{\alpha}}{p_{02}} \right) \left( \frac{\bar{\mu}^{\alpha}}{1 + \bar{r}^{\gamma\alpha}} \right)^{-1} & \text{for } s \notin S_1^{\alpha} \end{cases}$$

## Short-term Consumer Markets

$$(1 + r_{s^*}^{\gamma}) = \frac{\mu_{s^*}^{\alpha}}{m_{s^*}^{\gamma}}$$

$$(1 + r_{s^*}^{\delta}) = \frac{\mu_{s^*}^{\theta}}{m_{s^*}^{\delta}}$$

# Market Clearing Conditions

## Consumer Deposit Market

$$(1 + \bar{r}_d^\gamma) = \frac{\bar{\mu}_d^\gamma}{d^\theta}$$

## Wholesale Money Market

$$(1 + \bar{r}) = \frac{\bar{\mu}^\psi + \bar{\mu}^\phi}{\bar{m}}$$

## Repo Market

$$(1 + \rho_{s^*}^{CB}) = \frac{\mu_{s^*}^{G\delta}}{M_{s^*}^{CB} + d_{s^*}^{G\gamma}}$$

## Interbank Market

$$(1 + \bar{\rho}) = \frac{\bar{\mu}^\delta}{d^\gamma}$$

## MBS's Market

$$p^\alpha = \frac{\tilde{m}^\alpha}{\bar{m}^\alpha}$$

## CDO's Market

$$\tilde{q}^\alpha = \frac{\hat{m}^\alpha}{\tilde{m}^\alpha}$$

# Conditions on Expected Delivery Rates (Rational Expectations)

## Wholesale Money Market

$$\bar{R}_s = \begin{cases} \frac{\bar{v}_s^\psi \bar{\mu}^\psi + \bar{v}_s^\phi \bar{\mu}^\phi}{\bar{\mu}^\psi + \bar{\mu}^\phi} & \text{if } \bar{\mu}^\psi + \bar{\mu}^\phi > 0 \\ \text{arbitrary} & \text{if } \bar{\mu}^\psi + \bar{\mu}^\phi = 0 \end{cases} \quad \forall s \in S$$

## Interbank Market

$$\bar{R}_s^\delta = \begin{cases} \frac{\bar{v}_s^\delta \bar{\mu}^\delta}{\bar{\mu}^\delta} = \bar{v}_s^\delta & \text{if } \bar{\mu}^\delta > 0 \\ \text{arbitrary} & \text{if } \bar{\mu}^\delta = 0 \end{cases} \quad \forall s \in S$$



# Definition of Equilibrium

Let

$$\sigma^\alpha = (q_{s1}^\alpha, b_{s2}^\alpha, \mu_s^\alpha, \bar{\mu}^\alpha)$$

$$\sigma^\theta = (q_{s2}^\alpha, b_{s1}^\alpha, \mu_s^\theta, \bar{d}^\theta)$$

$$\sigma^\gamma = (\phi_s^\gamma, m_s^\gamma, d_s^{G\gamma}, \bar{m}^\alpha, \bar{\mu}_d^\gamma, \bar{d}^\gamma)$$

$$\sigma^\delta = (\phi_s^\delta, m_s^\delta, \mu_s^{G\gamma}, \bar{v}_s^\delta, \bar{m}, \bar{\mu}^\delta)$$

$$\sigma^\psi = (\bar{v}_s^\psi, \bar{\mu}^\psi, \tilde{m}^\alpha)$$

$$\sigma^\phi = (\bar{v}_s^\phi, \bar{\mu}^\phi, \hat{m}^\alpha)$$

$$\eta = (p_{s1}, p_{s2}, \rho_s^{CB}, r_s^\gamma, r_s^\delta, \bar{r}^{\gamma\alpha}, \bar{r}_d^\gamma, \bar{r}, \bar{\rho}, p^\alpha, \tilde{q}^\alpha)$$

Then  $(\sigma^\alpha, \sigma^\theta, \sigma^\gamma, \sigma^\delta, \sigma^\psi, \sigma^\phi, \eta)$  is a MEBCSD iff:

- ① All agents maximize given their budget sets
- ② All markets clear.
- ③ Expectations are rational.

# Credit Spreads

## Proposition 1

At any MEBCSD,  $r_{s^*}^\delta, \rho_{s^*}^{CB} \geq 0$ ,  $r_{s^*}^\delta = \rho_{s^*}^{CB} \quad \forall s^* \in S^*$ .

# Credit Spreads

## Proposition 1

At any MEBCSD,  $r_{s^*}^\delta, \rho_{s^*}^{CB} \geq 0, r_{s^*}^\delta = \rho_{s^*}^{CB} \quad \forall s^* \in S^*$ .

## Proposition 2

At any MEBCSD,  $r_{s^*}^\gamma, \rho_{s^*}^{CB} \geq 0, r_{s^*}^\gamma = \rho_{s^*}^{CB} \quad \forall s^* \in S^*$ .

# Credit Spreads

## Proposition 1

At any MEBCSD,  $r_{S^*}^\delta, \rho_{S^*}^{CB} \geq 0, r_{S^*}^\delta = \rho_{S^*}^{CB} \quad \forall s^* \in S^*$ .

## Proposition 2

At any MEBCSD,  $r_{S^*}^\gamma, \rho_{S^*}^{CB} \geq 0, r_{S^*}^\gamma = \rho_{S^*}^{CB} \quad \forall s^* \in S^*$ .

## Proposition 3

At any MEBCSD,  $\bar{r}_d^\gamma, \rho_0^{CB} \geq 0, \bar{r}_d^\gamma = \rho_0^{CB}$ .

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At any MEBCSD,  $r_{s^*}^{\gamma}, \rho_{s^*}^{CB} \geq 0$ ,  $r_{s^*}^{\gamma} = \rho_{s^*}^{CB} \quad \forall s^* \in S^*$ .

## Proposition 3

At any MEBCSD,  $\bar{r}_d^{\gamma}, \rho_0^{CB} \geq 0$ ,  $\bar{r}_d^{\gamma} = \rho_0^{CB}$ .

## Proposition 4

At any MEBCSD,  $p^{\alpha}, \rho_0^{CB} \geq 0$  and  $p^{\alpha} = 1 + \rho_0^{CB}$ .

# Credit Spreads

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At any MEBCSD,  $\bar{r}_d^\gamma, \rho_0^{CB} \geq 0$ ,  $\bar{r}_d^\gamma = \rho_0^{CB}$ .

## Proposition 4

At any MEBCSD,  $p^\alpha, \rho_0^{CB} \geq 0$  and  $p^\alpha = 1 + \rho_0^{CB}$ .

## Proposition 5

At any MEBCSD,  $\bar{r}, \bar{\rho}, \bar{r}_d^\gamma \geq 0$  and  $\bar{r} \geq \bar{\rho} \geq \bar{r}_d^\gamma$ .

# Term Structure of Interest Rates Proposition

## Proposition 6

At any MEBCSD for  $s \in S_1^\alpha$ ,

$$\sum_{j \in J} (m_0^j r_0^j) + \rho_0^{CB} \bar{m}^\alpha + \sum_{j \in J} (\pi_s^j) + \rho_s^{CB} M_s^{CB} + \rho_0^{CB} \bar{r}^{\gamma\alpha} \bar{m}^\alpha =$$

$$\sum_{h \in H} (e_{m,0}^h + e_{m,s}^h) + \sum_{\tilde{k}=\{\gamma,\delta,\psi\}} (e_0^k + e_s^k) + \frac{r_0^\gamma}{1+r_0^\gamma} \pi_0^\gamma$$

For  $s \notin S_1^\alpha$ ,

$$\sum_{j \in J} (m_0^j r_0^j) + \rho_0^{CB} \bar{m}^\alpha + \sum_{j \in J} (\pi_s^j) + \rho_s^{CB} M_s^{CB} + \rho_0^{CB} \bar{m}^\alpha (\bar{q}^\alpha - (1 + \bar{r}_s^{\gamma\alpha}))$$

$$= \sum_{h \in H} (e_{m,0}^h + e_{m,s}^h) + \sum_{\tilde{k}=\{\gamma,\delta,\psi\}} (e_0^k + e_s^k) + \frac{r_0^\gamma}{1+r_0^\gamma} \pi_0^\gamma$$

Put formally,  $\forall s \in S$  aggregate ex-post interest rate payments to commercial banks adjusted by default equal the economy's total amount of outside money plus interest payments of commercial banks' accumulated profits.











# Quantity Theory of Money Proposition

## Proposition 9 (continued)

For  $s \notin S_1^\alpha$

$$\sum_{h \in H, l = \{1,2\}} (p_{sl} q_{sl}^h) = \sum_{h \in H} e_{m,s}^h + \sum_{j \in J} e_s^j + M_s^{CB} + \pi_0^\gamma + \bar{R}_s \bar{m} (1 + \bar{r})$$

When there is default in the mortgage market, the quantity theory of money holds as in the previous case but the banking financial sector's loss due to default on the mortgage and derivatives markets is embedded in the expected repayment rates of wholesale money market loans.

## Proposition 9 (continued)

For  $s = 0$

$$\sum_{h \in H, l = \{1,2\}} (p_{0l} q_{0l}^h) = \sum_{h \in H} e_{m,0}^h + \sum_{j \in J} e_0^j + M_0^{CB} - \bar{m}$$

National income is equal to the stock of money in the economy less indirect expenditures by commercial banks in the derivatives markets.





# Discussion of the Equilibrium (continued)

- At  $s = 1$  no mortgage default, hence there's no default in wholesale money market
- At  $s = 2$ ,  $\alpha$  defaults on his mortgage
  - Significant losses in non-banking financial sector
  - CDS contract executed:  $\phi$  delivers collateral to  $\psi$  in exchange for initial investment value
  - $\psi$  assumes write down loss
- Economy becomes *financial unstable* at  $s = 2$ :
  - Default increases in wholesale and interbank markets
  - Banks' profits fall
- Monetary policy
  - Partially offsets effects of adverse productivity shock at  $s = 1$
  - Exacerbates effects of adverse productivity shock at  $s = 2$

















# Concluding Remarks

- In times of crisis, monetary policy conducted by means of the interest rate instrument is a more effective than using the monetary base instrument (See also Goodhart, Sunirand and Tsomocos, 2008)
- CPI should include an appropriate measure of housing prices
- Optimal regulatory policies should target systemic financial agents and induce them to behave more prudently before crises

